Reliability and validity of the Athens Insomnia Scale in chronic pain patients

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Purpose: To confirm the psychometric properties of the Athens Insomnia Scale (AIS) among Japanese chronic pain patients.

Patients and methods: In total, 144 outpatients were asked to complete questionnaires comprising the AIS and other study measures. According to the original article, the AIS has 2 versions: the AIS-8 (full version) and the AIS-5 (brief version). To validate the AIS-8 and AIS-5 among chronic pain patients, we confirmed: 1) factor structure by confirmatory factor analysis; 2) internal consistency by Cronbach’s α; 3) test–retest reliability using with interclass correlation coefficients; 4) known-group validity; 5) concurrent validity; and 6) cut-off values by receiver operating characteristic analysis. In addition, semi-structured interviews were conducted to assess the participants’ sleep disturbance. If the participants had any sleep complaints, including difficulty in initiating sleep, difficulty in maintaining sleep, and early morning awakening, they were defined as insomnia symptoms.

Results: A 2-factor model of the AIS-8 and 1-factor model of the AIS-5 demonstrated good fit. The AIS had adequate internal consistency and test–retest reliability. Patients with insomnia had a higher AIS score than those without insomnia. The sleep disturbance measured by the AIS was positively associated with pain intensity, disability, depression, anxiety, and pain catastrophizing, and negatively associated with pain-related self-efficacy. The cut-off values for detecting insomnia were estimated at 8 points in the AIS-8 and 4 points in the AIS-5.

Conclusion: The AIS-8 and AIS-5 had adequate reliability and validity in chronic pain patients.

Keywords: sleep disturbance, AIS, Japanese, insomnia symptom

Introduction

Sleep disturbance is a prevalent clinical complaint among individuals with chronic pain.1 In previous studies, 53%–89% of chronic pain patients had sleep complaints.2–6 Sleep disturbance is associated with greater pain intensity,3–6 disability,1 depression,3, 5, 6 and anxiety6 and also with pain-related cognition, such as greater pain catastrophizing and lower pain-related self-efficacy.7, 8 Therefore, the evaluation and treatment of sleep disturbance are essential components of pain management.9

A self-report questionnaire can be used to easily assess difficulties in the sleep of chronic pain patients. The Athens Insomnia Scale (AIS)10, 11 may be one of the useful measures because it assesses all 3 major insomnia symptoms (difficulties in initiating sleep [DIS], difficulties in maintaining sleep [DMS], and early morning awakening [EMA])12 and important sleep domains (sleep quality and quantity as well as daytime functioning).13 Furthermore, the AIS has only 8 items and takes few minutes to complete...
the AIS has been validated in patients with insomnia, psychiatric disorders, and cancer.\textsuperscript{10,14–16} However, it has not yet been validated in chronic pain patients.

This study aimed to validate the application of the AIS in chronic pain patients. According to the original author, the AIS has 2 versions: AIS-8 and AIS-5.\textsuperscript{10} The AIS-8 is the full version, which comprises 8 items related to both nocturnal sleep problems and daytime dysfunction. By contrast, the AIS-5 is the brief version of the AIS and comprises 5 items assessing only nocturnal sleep problems.\textsuperscript{10,14} We hypothesized that: 1) the score of AIS-8 and AIS-5 are positively associated with measures of pain intensity, disability, depression, anxiety, and pain catastrophizing; 2) they have negative correlations with pain-related self-efficacy measures; and 3) patients with insomnia symptoms have higher AIS-8 and AIS-5 scores than patients without insomnia symptoms.

Materials and methods

Participants

This study had a cross-sectional design. Outpatients on their first visit to a pain management center in a university hospital were included as participants. The data of this study were retrospectively extracted from the clinical records between April 2014 and December 2016.

The inclusion criteria were as follows: 1) a history of pain lasting for ≥3 months and 2) age ≥20 years. The exclusion criteria were as follows: 1) difficulty in reading and writing Japanese and 2) incomplete interview records of sleep disturbance. For example, if the frequency of DMS was not recorded, the author would be unable to assess the patient’s sleep condition.

Measures

AIS

The AIS-8 is an 8-item self-report questionnaire that measures the intensity of sleep difficulties\textsuperscript{10,11} according to the International Statistical Classification of Disease and Related Health Problems-10th Revision (ICD-10) diagnostic criteria for insomnia.\textsuperscript{14} Five items assess difficulty in sleep introduction, awakening during the night, early morning awakening, total sleep duration, and overall sleep quality. Three items pertain to the next-day consequences of insomnia (sense of well-being during the day, functioning [physical and mental] during the day, and sleepiness during the day). The AIS-5 is the brief version of the AIS-8 and comprises only 5 items assessing nocturnal sleep problems. Respondents are required to rate positively if they have experienced sleep difficulties at least thrice per week during the last month. Each item is rated on a 4-point numerical rating scale (NRS; where 0= no problem at all and 3= very serious problem). Total scores range from 0 to 24 in the AIS-8 and from 0 to 15 in the AIS-5. Higher scores in these AIS measures indicate that responders have severe insomnia symptoms.

The factor structure of the AIS-8 is different in populations. It has been reported as a 1-factor structure (item 1–8) or a 2-factor structure (item 1–5 and item 6–8) in previous studies.\textsuperscript{10,14,15,17} The factor structure of the AIS-5 is reported as a 1-factor structure only.\textsuperscript{14,15} Cronbach’s $\alpha$ coefficients for the Japanese version of the AIS-8 and AIS-5 were 0.88 and 0.85, respectively.\textsuperscript{14} The cut-off values for detecting insomnia among Japanese outpatients with chronic insomnia were estimated at 6 points in the AIS-8 and 4 points in the AIS-5.\textsuperscript{14}

NRS

To assess the pain intensity, we determined the average score of 4 items on an 11-point NRS. The NRS ranges from 0 (no pain) to 10 (worst pain imaginable), and the 4 assessed items are as follows: 1) worst pain in the past 24 hours; 2) least pain in the past 24 hours; 3) average pain in the past 24 hours; and 4) current pain. The average score of these 4 items was used for data analysis.\textsuperscript{19,20}

Pain Disability Assessment Scale (PDAS)

The PDAS is a self-report questionnaire assessing the degree of pain interference.\textsuperscript{21} It comprises 20 items, each of which is rated on a 4-point numerical rating scale. Higher scores (range from 0 to 60) indicate a greater degree of disability. Cronbach’s $\alpha$ coefficient of the total PDAS was 0.96.\textsuperscript{21}

Hospital Anxiety and Depression Scale (HADS)

The HADS is a 14-item self-report questionnaire, and each item is rated on a 4-point numerical rating scale. It comprises 2 subscales measuring anxiety (HADS-A) and depression (HADS-D).\textsuperscript{22} Each subscale includes 7 items, and higher scores indicate a greater degree of anxiety or depression. Total scores range from 0 to 42 and each subscale ranges from 0 to 21. Cronbach’s $\alpha$ coefficients for the Japanese version of the HADS were 0.77 for HADS-A and 0.79 for HADS-D.\textsuperscript{23,24} The cut-off value was estimated at 11 points in total score and 8 points in HADS-A and HADS-D.\textsuperscript{25}

Pain Catastrophizing Scale (PCS)

The PCS is a self-report questionnaire that assesses the degree of catastrophic thinking regarding pain. It comprises 13 items, each of which is rated on a 5-point numerical rating scale.
The PCS comprises 3 subscales: rumination, magnification, and helplessness. Higher scores indicate greater levels of catastrophizing. The total scores range from 0 to 51. The Japanese version of the PCS has good internal consistency (Cronbach’s α coefficients were 0.80 for the rumination subscale, 0.65 for the magnification subscale, 0.81 for the helplessness subscale, and 0.89 for the total score).

Pain Self-Efficacy Questionnaire (PSEQ)
The PSEQ is a 10-item self-report questionnaire that measures the confidence in performing activities despite pain. Each item is rated on a 7-point numerical rating scale. Higher scores indicate greater perceived self-efficacy among chronic pain patients. The total scores range from 0 to 60. The Cronbach’s α coefficient for the Japanese version of the PSEQ was 0.94.

Patient’s Global Impression of Change (PGIC)
The PGIC is a self-report questionnaire that measures the change in patients’ overall conditions since treatment initiation. It is a 7-point categorical scale and is scored as follows: 1) very much improved; 2) much improved; 3) minimally improved; 4) no change; 5) minimally worse; 6) much worse; and 7) very much worse. Participants who visited the hospital again were asked to complete this questionnaire. In the present study, we used the PGIC for assessing the test–retest reliabilities of the AIS-8 and AIS-5.

Semi-structured interview for sleep disturbance
In a semi-structured interview conducted by psychologists, participants were questioned regarding their sleep condition. The items assessed through the interview were wake-up time, bedtime, DIS, DMS, EMA, and history of sleeping pill consumption. DIS was defined as requiring >30 min to fall asleep; the presence of DMS and EMA was defined as ≥3 episodes per week. The presence of insomnia was defined as at least 1 positive response to questions regarding DIS, DMS, or EMA.

Procedure
Data were collected as part of routine care at a tertiary pain management center. First, the participants were informed that their questionnaire data and clinical records might be used for clinical and research purposes. If the participants agreed, they were asked to complete questionnaires using an e-tablet with a touch screen in the waiting room. After completing the questionnaires, the patients were consulted by a multidisciplinary team (physician, occupational therapist, physiotherapist, and psychotherapist). During the psychological assessment, the psychologist conducted semi-structured interviews regarding the sleep condition. The interviews were conducted by either of two psychotherapists. Patients who revisited the clinic within 100 days were asked to complete the questionnaires twice. This study was approved by the Institutional Review Board of the Osaka University Hospital (No. 13004-6), and written informed consent was obtained from all participants prior to study inclusion.

Statistical analysis
All statistical analyses were conducted using R software (version 3.4.1). Descriptive statistics were calculated to describe the demographic characteristics of the participants. The factor structures of the AIS-8 and AIS-5 were analyzed through confirmatory factor analysis using the package “lavaan” (version 0.5-23). To determine absolute fit indices, the chi-square goodness-of-fit index (χ²), the root mean square error of approximation (RMSEA), and the standardized root mean square residual (SRMR) were used. An acceptable fitting model was determined as that with a 0.05 threshold using non-significant χ² tests, with a RMSEA of <0.08, and a SRMR of <0.10. To assess incremental fit indices, the comparative fit index (CFI) was used. An acceptable model was determined as that with a CFI of >0.95. In addition, the Akaike Information Criterion (AIC) was used as a parsimony fit index. The best model demonstrated the minimal value of AIC. The χ² improvement was assessed between the 2 nested models of the AIS-8.

Internal consistencies in the AIS-8 and AIS-5 were evaluated using Cronbach’s α. Test–retest reliability was determined in participants who responded with scores of 3 (minimally improved), 4 (no change), or 5 (minimally worse) on the PGIC at the second visit. To assess test–retest reliability, the interclass correlation coefficient (ICC) was calculated. By using the Pearson correlation coefficients, concurrent validity was evaluated between the AIS and other psychometric measures (the NRS, PDAS, HADS, PCS, and PSEQ) for all participants. Known-group validity was established using the independent t-test to compare the mean values of AIS scores between participants with insomnia and those without insomnia defined by semi-structured interview. In the present study, the significance level was set at p<0.05. Finally, the cut-off points for the AIS-8 and AIS-5 were established with receiver-operating characteristic (ROC) curves using the package “pROC” (version 1.10.0). The optimal cut-off value was determined based on the sensitivity and specificity.
for all participants. The diagnostic accuracy was evaluated by calculating the area under the curve (AUC). Generally, an AUC of 0.9–1.0 represents excellent, 0.8–0.9 represents good, 0.7–0.8 represents fair, and 0.6–0.7 represents poor discriminative ability.40

**Results**

**Demographic characteristics of participants**

In total, 144 participants completed the questionnaires and semi-structured interviews. Demographic valuables are shown in Table 1. Eighty-six participants were females (60.0%), and the mean age was 53.3 (SD=16.2) years. The average pain duration was 53.6 (SD=66.7) months. The most frequently reported pain sites were the lower limbs (68.1%), followed by upper shoulder and upper limbs (55.6%), and the lower back (51.4%). Furthermore, 45.0% of the participants reported experiencing pain at more than 3 sites. Participants were classified using the recently proposed International Association for the Study of Pain classification.41,42 A total of 61.8% of participants were categorized as Code 1 (chronic primary pain).

Most participants (88.9%) had received at least high school education. Marital status was as follows: married (52.8%), single (25.0%), divorced (12.5%), remarried (4.1%), and widowed (5.6%). Only 33.4% of the participants were working. A total of 50.0% of participants took medication for difficulty sleeping. The prevalence of DIS was 47.9%, of DMS was 75.7%, and of EMA was 18.1%. In total, 131 participants (91.0%) exhibited insomnia symptoms. The mean AIS-8 score was 10.8 (SD=5.7), mean AIS-5 score was 6.7 (SD=4.1), and mean daytime function (items 6–8) score was 4.1 (SD=2.3). The scores for other questionnaires are reported in Table 2.

**Confirmatory factor analysis**

Fit indices revealed that the 1-factor model of the AIS-8 was a poor fit to the data: \(\chi^2 (20)=121.315, p<0.001\), SRMR =0.082, RMSEA =0.188 (90% CI: 0.157–0.221), CFI =0.840, and AIC =2687.137. Conversely, the 2-factor model of the AIS-8 was an acceptable fit to the data: \(\chi^2 (19)=36.325, p<0.05\), SRMR =0.045, RMSEA =0.080 (90% CI: 0.039–0.119), CFI =0.973, and AIC =2623.297. Furthermore, the model fit significantly improved for the 2-factor model (\(\Delta\chi^2 [1]=84.99; p<0.001\)). Therefore, we adopted the 2-factor structure for the AIS-8 (Figure 1). The factor loading for item 8 was low in the 2-factor model. However, the fit indices were poor if item 8 was removed: \(\chi^2 (13)=32.852, p<0.01\), SRMR =0.051, RMSEA =0.103 (90% CI: 0.060–0.148), and CFI =0.949. Thus, the 2-factor model retaining item 8 was finally selected.

For the AIS-5, fit indices revealed that the 1-factor model was marginally acceptable: \(\chi^2 (5)=12.495, p<0.05\), SRMR =0.045, RMSEA =0.102 (90% CI: 0.031–0.175), CFI =0.983, and AIC =1602.073. To improve the model fit, modification indices suggested the addition of error covariances between items 1 and 5. These items provide a more subjective evaluation of nocturnal sleep problems than items 2–4. Therefore,
items 1 and 5 were permitted to covary. With the addition of this error covariance, the model showed a good fit: \( \chi^2 (4) = 4.007, p = 0.41, \) SRMR = 0.013, RMSEA = 0.004 (90% CI: 0.000–0.126), CFI = 1.000, and AIC = 1595.526 (Figure 2).

### Internal consistency and test–retest reliability

Cronbach’s \( \alpha \) coefficient for the AIS-8 total score was 0.87 and the AIS-5 was 0.89. In subscales, Cronbach’s \( \alpha \) coefficient was 0.89 for nocturnal sleep problems and 0.66 for daytime dysfunction. Test–retest reliability was analyzed in 43 participants (19 males and 24 females). The mean period between the first and second surveys was 81.4 (SD = 19.3; range = 21–98) days. The overall ICC was 0.64 (95% CI: 0.43 to 0.79) for the AIS-8, 0.72 (95% CI: 0.45 to 0.80) for the AIS-5 and nocturnal sleep problems, and 0.54 (95% CI: 0.29 to 0.72) for daytime dysfunction.

### Concurrent validity

Correlation analyses revealed that the AIS-8 had moderate correlations with the PDAS, HADS-A, HADS-D, and PSEQ, and the AIS-5 had moderate correlations with the HADS-A and HADS-D. Moreover, the AIS-8 was weakly associated with the NRS and PCS, and the AIS-5 had weak correlations with the NRS, PDAS, PCS, and PSEQ (Table 3).
Known-group validity

Based on the semi-structured interview data, the participants were divided into an insomnia group (n=131) and non-insomnia group (n=13). The mean AIS-8 score was 11.4 (SD =5.6) for those with insomnia and 5.2 (SD =3.4) for those without insomnia. In addition, the mean AIS-5 score was 7.1 (SD =4.0) in participants with insomnia and 2.7 (SD =2.5) in participants without insomnia. Independent t-tests revealed higher AIS scores in participants with insomnia than in those without insomnia in both the AIS-8 and AIS-5 (AIS-8: t=3.93, df=142, p<0.001; AIS-5: t=3.81, df=142, p<0.001).

Cut-off point

Based on the ROC analysis, the cut-off value of the AIS-8 for insomnia was estimated at 8 points, with 72% sensitivity and 85% specificity. Furthermore, the cut-off value of the AIS-5 was estimated at 4 points, with 78% sensitivity and 70% specificity (Table 4). The AUC was 0.82 (95% CI: 0.72 to 0.91) for the AIS-8 and 0.82 (95% CI: 0.71 to 0.92) for the AIS-5. The ROC curves are shown in Figure 3.

Discussion

The present study aimed to examine the psychometric properties of the AIS-8 and AIS-5 in Japanese chronic pain patients.

**Table 3** Correlation coefficients between AIS and the other psychological measures

<table>
<thead>
<tr>
<th>Measure</th>
<th>AIS-8 (95% CI)</th>
<th>AIS-5 (95% CI)</th>
</tr>
</thead>
<tbody>
<tr>
<td>NRS</td>
<td>0.36 (0.21 to 0.50)</td>
<td>0.35 (0.19 to 0.48)</td>
</tr>
<tr>
<td>PDAS</td>
<td>0.46 (0.33 to 0.58)</td>
<td>0.37 (0.22 to 0.51)</td>
</tr>
<tr>
<td>HADS-anxiety</td>
<td>0.54 (0.41 to 0.65)</td>
<td>0.42 (0.28 to 0.55)</td>
</tr>
<tr>
<td>HADS-depression</td>
<td>0.64 (0.53 to 0.73)</td>
<td>0.52 (0.39 to 0.63)</td>
</tr>
<tr>
<td>PCS-total</td>
<td>0.36 (0.21 to 0.49)</td>
<td>0.26 (0.10 to 0.41)</td>
</tr>
<tr>
<td>PCS-rumination</td>
<td>0.23 (0.07 to 0.38)</td>
<td>0.17 (0.01 to 0.33)</td>
</tr>
<tr>
<td>PCS-magnification</td>
<td>0.37 (0.22 to 0.50)</td>
<td>0.27 (0.11 to 0.42)</td>
</tr>
<tr>
<td>PCS-helplessness</td>
<td>0.35 (0.19 to 0.48)</td>
<td>0.24 (0.08 to 0.39)</td>
</tr>
<tr>
<td>PSEQ</td>
<td>−0.47 (−0.59 to −0.33)</td>
<td>−0.35 (−0.48 to −0.19)</td>
</tr>
</tbody>
</table>

Abbreviations: AIS, Athens Insomnia Scale; HADS, hospital anxiety and depression scale; NRS, numerical rating scale; PDAS, pain catastrophizing scale; PCS, pain disability assessment scale; PSEQ, pain self-efficacy questionnaire.

**Table 4** Sensitivity and specificity values of the AIS

<table>
<thead>
<tr>
<th>Measure</th>
<th>Cut-off score</th>
<th>Sensitivity (%)</th>
<th>Specificity (%)</th>
<th>AUC (95% CI)</th>
</tr>
</thead>
<tbody>
<tr>
<td>AIS-8</td>
<td>7</td>
<td>75</td>
<td>69</td>
<td>0.82 (0.72 to 0.91)</td>
</tr>
<tr>
<td></td>
<td>8</td>
<td>72</td>
<td>85</td>
<td></td>
</tr>
<tr>
<td></td>
<td>9</td>
<td>66</td>
<td>85</td>
<td></td>
</tr>
<tr>
<td>AIS-5</td>
<td>3</td>
<td>83</td>
<td>46</td>
<td>0.82 (0.71 to 0.92)</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>78</td>
<td>70</td>
<td></td>
</tr>
<tr>
<td></td>
<td>5</td>
<td>69</td>
<td>76</td>
<td></td>
</tr>
</tbody>
</table>

Note: *Optimal cutoff score values are shown in bold.

Abbreviations: AIS, Athens Insomnia Scale; AUC, area under the curve.
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catastrophizing, and negatively associated with self-efficacy in the current study. In previous studies, sleep disturbance was associated with greater pain intensity,3–6 disability,7 depression,3,5,6 anxiety,6 and pain catastrophizing.7 In addition, poor sleep quality was associated with worse levels of self-efficacy in patients with fibromyalgia.8 Therefore, the correlation between the AIS and other psychometric questionnaires is applicable. Concurrent validity was confirmed for the AIS. The cut-off value of the AIS-8 was higher than that of the original and Japanese versions (6 points for both) for an insomnia sample.10,14 By contrast, the cut-off value of the AIS-5 was the same as that of the Japanese version for patients with insomnia.14 The cut-off value of only the AIS-8 was higher than that of the original version because the current participants with chronic pain might have rated their daytime dysfunction (items 6–8) more positively than participants with primary insomnia. Actually, the mean daytime dysfunction score in this study was higher than that of the primary insomnia group (3.65; SD = 1.95).14 According to Dueñas’s review, chronic pain severely affects the patients’ daily activities and quality of life.41 Many chronic pain patients are less able to exercise, walk, work outside home, attend social activities, and do household chores.2 Hence, because of pain, chronic pain patients with insomnia would feel more daytime dysfunction than patients with primary insomnia.

Limitations

This study has some limitations. First, the number of patients without insomnia is low (N=13), and the selection bias might have occurred in this study. The low number of non-insomnia patients may be due to the participants in this study being recruited in a tertiary care setting, in which many patients may experience severe pain and insomnia. In previous studies, 92.9% chronic pain patients reported difficulty with sleep in tertiary setting,4 while 74.9% patients with chronic pain reported sleep disturbance in primary care settings.44 The patients in current study would experience more insomnia than those in primary or secondary care settings.

Second, this study did not apply any other insomnia scales (such as the Pittsburgh Sleep Quality Index45 and Insomnia Severity Index46) or objective measures of sleep (e.g., actigraphy and polysomnography). In previous studies, other insomnia scales and Actiwatch parameters have been measured to confirm the validity of the AIS.14,16,17 Furthermore, the semi-structured interview for insomnia was brief. The diagnostic criteria of Diagnostic and Statistical Manual of Mental Disorders-IV-Text Revision were used to divide participants into insomnia and non-insomnia groups in previous studies.16,17

In spite of these limitations, we confirmed good psychometric properties of the AIS in chronic pain patients. The AIS is widely used for assessing the risk of insomnia,12 because it is short and assesses important sleep domain.12,13 The AIS is expected to assess insomnia symptom of chronic pain patients not only in research settings, but also in clinical settings.

Conclusion

This study demonstrated that the AIS-8 and AIS-5 have excellent reliability and validity in chronic pain patients.
The cut-off value for screening insomnia was estimated at 8 points in the AIS-8 and 4 points in the AIS-5. The AIS has high utility because it assesses all the 3 major insomnia symptoms and takes only a few minutes to complete. The AIS is useful for assessing insomnia symptoms of chronic pain patients in research and clinical practice.

**Author contributions**
All authors contributed toward data analysis, drafting and revising the paper and agree to be accountable for all aspects of the work.

**Disclosure**
The author reports no conflicts of interest in this work.

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