Effective heating of magnetic nanoparticle aggregates for in vivo nano-theranostic hyperthermia

Chencai Wang¹
Chao-Hsiung Hsu¹,²
Zhao Li³
Lian-Pin Hwang²
Ying-Chih Lin²
Pi-Tai Chou²
Yung-Ya Lin¹

¹Department of Chemistry and Biochemistry, University of California, Los Angeles, CA, USA; ²Department of Chemistry, National Taiwan University, Taipei, Taiwan

Abstract: Magnetic resonance (MR) nano-theranostic hyperthermia uses magnetic nanoparticles to target and accumulate at the lesions and generate heat to kill lesion cells directly through hyperthermia or indirectly through thermal activation and control releasing of drugs. Preclinical and translational applications of MR nano-theranostic hyperthermia are currently limited by a few major theoretical difficulties and experimental challenges in vivo conditions. For example, conventional models for estimating the heat generated and the optimal magnetic nanoparticle sizes for hyperthermia do not accurately reproduce reported in vivo experimental results. In this work, a revised cluster-based model was proposed to predict the specific loss power (SLP) by explicitly considering magnetic nanoparticle aggregation in vivo conditions. By comparing with the reported experimental results of magnetite Fe₃O₄ and cobalt ferrite CoFe₂O₄ magnetic nanoparticles, it is shown that the revised cluster-based model provides a more accurate prediction of the experimental values than the conventional models that assume magnetic nanoparticles act as single units. It also provides a clear physical picture: the aggregation of magnetic nanoparticles increases the cluster magnetic anisotropy while reducing both the cluster domain magnetization and the average magnetic moment, which, in turn, shift the predicted SLP toward a smaller magnetic nanoparticle diameter with lower peak values. As a result, the heating efficiency and the SLP values are decreased. The improvement in the prediction accuracy in vivo conditions is particularly pronounced when the magnetic nanoparticle diameter is in the range of ~10–20 nm. This happens to be an important size range for MR cancer nano-theranostics, as it exhibits the highest efficacy against both primary and metastatic tumors in vivo. Our studies show that a relatively 20%–25% smaller magnetic nanoparticle diameter should be chosen to reach the maximal heating efficiency in comparison with the optimal size predicted by previous models.

Keywords: nano-theranostics, hyperthermia, magnetic resonance, magnetic nanoparticle, specific loss power

Introduction

Theranostics refers to the development of molecular diagnostics and targeted therapeutics in an interdependent, collaborative manner. Nano-theranostics takes advantage of the high capacity of nano-platforms to ferry cargo and load onto them both imaging and therapeutic functions. The resulting nanosystems, capable of diagnosis, drug delivery, and monitoring of therapeutic response, are expected to play a significant role in the dawning era of personalized medicine, and much research effort has been devoted toward that goal. For example, magnetic resonance (MR) nano-theranostics uses magnetic nanoparticles for cancer detection by MR imaging
and for cancer therapy by MR nano-medicine. Through active (e.g. antibody–antigen) and passive (e.g. enhanced permeability and retention effect) targeting mechanisms, the magnetic nanoparticles can serve as “molecular beacons” to enhance the MR image contrast for early lesion detection. Moreover, through interacting with external alternating magnetic fields produced by the MR hardware, these magnetic nanoparticles accumulated at the lesions can generate heat to serve as “molecular bullets” to kill cancer cells directly through hyperthermia or indirectly through thermal activation and control releasing of drugs.

MR nano-theranostic hyperthermia with magnetic nanoparticles has been an emerging field for the last decade, mainly for its promising applications to cancer treatment. In particular, a number of studies have shown that these magnetic fluids, or magnetic nanoparticle suspensions, are able to release heat through various relaxation mechanisms when exposed to a weak alternating magnetic field. The selective heating can be used to target cancer tissues, as abnormal growth is more susceptible to cell death under elevated temperatures. However, preclinical and translational applications of MR nano-theranostic hyperthermia with magnetic nanoparticles are limited by a few major theoretical difficulties and experimental challenges. For example, conventional theoretical models for MR nano-theranostic hyperthermia assume that the magnetic nanoparticles act independently as single units and are dispersed uniformly in the colloidal suspension, making the interaction among the nanoparticles negligible. However, in real biomedical in vivo applications, when magnetic nanoparticles have been injected into blood vessels or bound to cancer cells through the antibody–antigen interaction, individual nanoparticles are highly likely to aggregate and form clusters.

Aggregation changes the physical and magnetic properties of the magnetic nanoparticles in tissues, such as magnetic susceptibility and specific loss power (SLP). Furthermore, aggregate formation and disruption were found to be affected by external magnetic field conditions. Consequently, a higher magnetic field strength is required to disrupt these aggregates, lowering the heating efficiency of the magnetic nanoparticles in tissues. Therefore, further understanding and formulation of the effect of magnetic nanoparticle aggregation on MR nano-theranostic hyperthermia becomes critical.

To understand and optimize MR nano-theranostic hyperthermia using magnetic nanoparticles, the SLP lays a constructive platform for calculating the heat generation per mass unit of dissipating material. SLP is shown to depend on magnetic nanoparticle properties and external alternating magnetic fields, specifically the mean particle size and size distribution, as well as the amplitude and frequency of the alternating magnetic fluids. Therefore, reaching a therapeutic temperature for cancer treatment while administering minimal amounts of magnetic nanoparticles, due to limited targeting efficiency, would thus depend greatly on manipulating magnetic-nanoparticle properties and external alternating magnetic fields to control the desired SLP and heat generated. Problematically, conventional models for estimating SLP do not accurately reproduce reported experimental results. This limitation may be alleviated by analyzing the magnetic nanoparticle composition and structure under experimental conditions.

The original model proposed by Rosensweig assumes magnetic nanoparticles act independently of one another in suspension. Morais et al and Castro et al found magnetic nanoparticles form clusters when in solution. Ganguly et al reported experimental observation on the micro- and meso-scale field-assisted self-assembly of magnetic nanoparticles due to interparticle electrostatic attraction, electrostatic repulsion, steric repulsion, and magnetic dipolar interactions. Interestingly, several groups have determined that magnetic nanoparticle aggregate formation is not sensitive to the solution composition, as magnetic nanoparticles were found to form aggregates in similar magnitudes when suspended in either water or glycerol. Furthermore, magnetic fluid characteristics and structures differ under varying alternating magnetic field strengths, such that the fraction of agglomerates changes the magnetization and susceptibility of the ferrofluid.

In this work, we proposed a revised cluster-based model to more accurately estimate the SLP by considering magnetic nanoparticle aggregation. Under an alternating magnetic field, magnetic susceptibility is temperature dependent and can be conveniently described by the Langevin function. The fraction of monomeric and clustered magnetic nanoparticles in the ferrofluid can be characterized by a critical temperature, which is defined as the temperature at which magnetic nanoparticle aggregates completely dissociate into individual units. To account for dependence on this critical temperature, we proposed a modified Langevin function to redefine the magnetic susceptibility of the ferrofluid and developed an alternative SLP model based on the revised Langevin function. The proposed model, called “revised cluster-based model,” can account for the aggregate formation and the size distribution of the magnetic nanoparticles. Finally, the proposed model was compared with experimental results of magnetite Fe₃O₄ and cobalt ferrite CoFe₂O₄ magnetic
nanoparticles.\textsuperscript{22–25} It is shown that the revised cluster-based model provides more accurate estimates of SLP and heating efficiency for MR nano-theranostic hyperthermia in cancer therapy.

**Materials and methods**

**Fraction of monomers and clusters**

The disruption of magnetic nanoparticle clusters follows a second-order phase transition at the critical temperature.\textsuperscript{14} Magnetic nanoparticle monomers and clusters coexist within the colloidal solution when the temperature of the ferrofluid is below the critical temperature. Correspondingly, clusters disrupt completely into monomeric units when the ferrofluid temperature is at or above the critical temperature. Therefore, the fraction of clusters \( P_c \) in the ferrofluid was chosen as an order parameter to describe this thermal-assisted cluster disruption, according to the Landau second-order phase transition theory, where \( P_c \) was expressed in terms of the suspension temperature, \( T \), and the critical temperature, \( T^* \).\textsuperscript{21}

\[
P_c = \left(1 - \frac{T}{T^*}\right)^{\frac{1}{2}} \quad (1A)
\]

From the expression of \( P_c \), it can be concluded that when the temperature is much lower than the critical temperature, \( T \ll T^* \), monomers and clusters coexist in the ferrofluid system, and there are no clusters when the temperature is at or above the critical temperature. Consequently, the fraction of monomers \( P_m \) in the ferrofluid can be simply treated to be proportional to the temperature:

\[
P_m = \frac{T}{T^*} \quad (1B)
\]

Notice that \( P_m + P_c = 1 \) when it is at two limiting conditions: \( T \ll T^* \) and \( T \approx T^* \).

**Relaxation mechanisms**

To calculate the SLP of colloidal magnetic nanoparticles as an interacting system in ferrofluid, we first need to describe two major relaxation mechanisms for magnetic nanoparticles dispersed in a fluid. The first relaxation mechanism is referred to as the Brownian relaxation and was first derived by Debye.\textsuperscript{26} It assumes the whole nanoparticle rotates toward the external field mechanically against the viscous drag in the suspending medium. Consequently, the change in the magnetization of a ferrofluid is due to the rotation of the magnetic nanoparticles with the internal magnetization remaining fixed with respect to the crystalline lattice. For this reason, it is also known as the “rigid dipole model.” Assuming that the viscosity of the ferrofluid solution, \( \eta \), is temperature independent and the effect of the magnetic nanoparticle aggregation does not depend on the suspending solution, one can derive the characteristic zero-field Brownian relaxation time constant, \( \tau_B \), to be:

\[
\tau_B = \frac{3 \eta V a}{k_B T} \quad (2)
\]

where the magnetic nanoparticle’s hydrodynamic volume \( V = (1 + \delta R)V \), \( k_B \) is the Boltzmann constant, \( T \) is the temperature of the ferrofluid solution (the product \( k_B T \) is the thermal energy), \( \eta \) is the viscosity of the carrier fluid, \( V \) is the volume of the magnetic nanoparticle, \( R \) is the radius of the magnetic nanoparticle, and \( \delta \) is the surfactant thickness (a property of the ferrofluid).

The second relaxation mechanism, known as the Néel relaxation, describes a process where the magnetic nanoparticles do not mechanically rotate, but the magnetization rotates internally with respect to the crystalline lattice.\textsuperscript{27} Because of the nanoparticle’s magnetic anisotropy, the magnetization has usually two stable orientations antiparallel to each other, separated by an energy barrier. The stable orientations define the magnetic easy axis of the nanoparticle. Because the magnetization rotates away from the easy axis toward the external field in the Néel relaxation process, the mechanism is also known as the “soft dipole model.” The characteristic zero-field Néel relaxation time constant, \( \tau_N \), can be expressed as:

\[
\tau_N = \begin{cases} 
\tau_0 \Gamma^{-\frac{1}{2}} \exp(\Gamma) & \Gamma \geq 1 \\
\tau_0 \Gamma & \Gamma \ll 1 
\end{cases} \quad (3)
\]

where \( \Gamma = \frac{K V}{k_B T} \), \( K \) is the energy barrier (a product of the magnetic anisotropy constant, \( K_m \), and the volume of the magnetic nanoparticle, \( V \)), and \( \tau_0 \) is the attempt time (its reciprocal is called the attempt frequency). Typical values for \( \tau_N \) are between \( 10^{-9} \) and \( 10^{-10} \) s.

Because both relaxation mechanisms occur simultaneously in the ferrofluid, the effective total relaxation time constant, \( \tau \), is given by:

\[
\frac{1}{\tau} = \frac{1}{\tau_B} + \frac{1}{\tau_N} \quad (4A)
\]
or, alternatively, by:

\[ \tau = \frac{\tau_a \cdot \tau_N}{\tau_a + \tau_N} \]  

(4B)

When \( \tau_a \ll \tau_N \), \( \tau = \tau_N \). Similarly, when \( \tau_a \gg \tau_N \), \( \tau = \tau_a \). Hence, the total relaxation effect is dominated by the stronger relaxation mechanism with shorter relaxation time constant.

Since aggregation increases the magnetic anisotropy of clusters,\(^{28-30}\) in our proposed model, the magnetic anisotropy constant, \( K_a \), has different values for monomers and clusters. If we denote the magnet anisotropy constants for monomers and clusters as \( K_{mm} \) and \( K_{ac} \), respectively, then:

\[ K_{ac} = K_{mm} + \frac{(1 - P_a)K_a}{P_c} \]  

(5B)

where the term \( \frac{(1 - P_a)K_a}{P_c} \) represents the increase in the average of the magnetic anisotropy constant due to the formation of clusters, and \( 1 - P_a \) represents the fraction of monomers that comes from the disruption of clusters. It should be noted that when \( T \) is close to \( T^* \), the value of \( K_{ac} \) is slightly higher than that of \( K_{mm} \), and when \( T \ll T^* \), the complicated structure of clusters makes \( K_{ac} \) significantly higher than \( K_{mm} \).

**Equilibrium magnetization**

In this work, we investigated the effect of magnetic nanoparticle aggregation on the magnetization and the magnetic susceptibility of ferrofluid. Considering the linear response of the magnetic susceptibility, one can rewrite the equilibrium magnetization of ferrofluid as a function of the temperature, \( M_0(T) \), as:\(^{31}\)

\[ M_0(T) = \phi \left[ M_{dm} \left( \frac{T}{T^*} \right)^{1/2} L \left( \frac{\mu_0 m H_0}{k_B T} \right) + M_{dc} \left( 1 - \frac{T}{T^*} \right)^{1/2} L \left( \frac{\mu_0 m H_0}{k_B T} \right) \right] \]  

(6)

where \( \frac{T}{T^*} = P_a \) and \( \left( 1 - \frac{T}{T^*} \right)^{1/2} = P_c \) are the fractions of monomers and clusters, respectively, as shown in equation 1; \( \phi \) is the volume fraction of the magnetic nanoparticles; \( H_0 \) is the strength of the external alternating magnetic field; \( \mu_0 \) is the magnetic permeability in free space; \( M_{dm} \) and \( M_{dc} \) are the domain magnetization of monomers and clusters, respectively; \( \overline{m}_m \) and \( \overline{m}_c \) are the average magnetic moment of monomers and clusters, respectively; and \( L \) is the Langevin function with formula \( L(x) = \coth(x) - \frac{1}{x} \). The Langevin function describes the dependency of the magnetization on the applied magnetic field in the classical limit, with the expression:

\[ L \left( \frac{\mu_0 m H_0}{k_B T} \right) = \coth \left( \frac{\mu_0 m H_0}{k_B T} \right) - \frac{k_B T}{\mu_0 m H_0} \]  

(7A)

\[ L \left( \frac{\mu_0 m H_0}{k_B T} \right) = \coth \left( \frac{\mu_0 m H_0}{k_B T} \right) - \frac{k_B T}{\mu_0 m H_0} \]  

(7B)

In equation 6, the first term in the parentheses indicates the contribution from monomers, while the second term in the parentheses indicates the contribution from clusters. Similar to the effect of magnetic nanoparticle aggregation on the magnetic anisotropy constant, the domain magnetization \( M_m \) and the average magnetic moment \( \overline{m}_c \) of clusters are also different from those of monomers:

\[ M_{dc} = \frac{(1 - P_a)M_{dm}}{P_c} \]  

(8A)

\[ \overline{m}_c = \frac{(1 - P_a)\overline{m}_m}{P_c} \]  

(8B)

where \( M_{dm} \) and \( \overline{m}_m \) are the domain magnetization and the average magnetic moment of monomers, respectively. While aggregation increases the magnetic anisotropy constant for clusters, \( K_{ac} \) (equation 5B), it decreases both the domain magnetization \( M_m \) and the average magnetic moment \( \overline{m}_c \) for clusters (equations 8A and B), due to the minimization of internal energy.\(^{11}\) Consequently, in this work, the effect of the magnetic nanoparticle aggregation is modeled through a corrected expression for the actual magnetization using a revised Langevin function.

**Magnetic susceptibility**

In the presence of an alternating magnetic field of the form

\[ H(t) = H_0 \cos(\omega t) = \text{Re}[H_0 e^{i\omega t}] \]  

(9A)

the magnetization, \( M(t) \), lags the magnetic field, \( H(t) \). Therefore, it is convenient to express the magnetization in
terms of the complex magnetic susceptibility, \( \chi = \chi' - i\chi'' \), resulting in:

\[
M(t) = \text{Re}[\chi H_0 e^{i\omega t}] = H_0 (\chi' \cos \omega t + \chi'' \sin \omega t) \quad (9B)
\]

As can be derived from the Shilomis relaxation equations, when an alternating magnetic field is applied to the ferrofluid, the dynamics of the magnetization, \( M(t) \), is governed by:

\[
\frac{\partial M(t)}{\partial t} = \frac{1}{r} (M_0(t) - M(t)) \quad (10A)
\]

where the equilibrium magnetization, \( M_0(t) \), under the alternating magnetic field can be expressed as:

\[
M_0(t) = \chi_o(T) H_0 \cos(\omega t) = \text{Re}[\chi_o(T) H_0 e^{i\omega t}] \quad (10B)
\]

where \( \chi_o(T) \) is the equilibrium magnetic susceptibility. Substituting equations 9B and 10B into equation 10A yields:

\[
-\omega \chi'' \sin(\omega t) + \omega \chi' \cos(\omega t) = (\chi_o(T) - \chi') \cos(\omega t) - \chi'' \sin(\omega t) \quad (10C)
\]

Comparing the corresponding coefficients, we can obtain the expression for both the real part and the imaginary part of the complex magnetic susceptibility, \( \chi \):

\[
\chi' = \frac{\chi_o(T)}{1 + (\omega r)^2} \quad (11A)
\]

\[
\chi'' = \frac{\omega \chi'_o(T)}{1 + (\omega r)^2} \quad (11B)
\]

where the equilibrium magnetic susceptibility, \( \chi_o(T) \), can be derived from the expression for the equilibrium magnetization of ferrofluid (equation 6):

\[
\chi_o(T) = \frac{M_o(T)}{H_0} = \frac{\varphi}{H_0} \left[ M_{\varphi} \left( \frac{T}{T^*} \right) L \left( \frac{\mu_o m H_o}{k_B T} \right) + M_{\sigma} \left( 1 - \frac{T}{T^*} \right) \frac{1}{2} L \left( \frac{\mu_o m H_o}{k_B T} \right) \right] \quad (12)
\]

### Power dissipation

Using the equilibrium magnetization, \( M_0(T) \) from equation 6 and the equilibrium magnetic susceptibility, \( \chi_o(T) \), from equation 12, we are ready to calculate the adjusted power dissipation. For magnetic nanoparticles suspended in an alternating magnetic field, the energy dissipation is equal to the change in the internal energy, \( \Delta U \), or equivalently, the loss of the magnetic work:\

\[
\Delta U = -\mu_0 \oint M(t) dH \quad (13A)
\]

\[
\Delta U = -\frac{\pi}{\mu_0} \text{Re}[\chi H_0 e^{-i\omega t}] dH \quad (13B)
\]

\[
\Delta U = \mu_0 \pi H_0^2 \chi'' \quad (13C)
\]

Substituting equation 11B and \( \omega = 2\pi f \) into equation 13C, we obtain the final expression for the change in the internal energy, \( \Delta U \):

\[
\Delta U = \frac{2\mu_0 H_0^2 f \pi^2 \chi'_o(T)}{1 + (2\pi f \tau)^2} \quad (13D)
\]

Using the change in the internal energy, \( \Delta U \), the volumetric power dissipation, \( P \), can be expressed as:

\[
P = f \Delta U = f \mu_0 \pi H_0^2 \chi'' \quad (14A)
\]

which is derived from the integration and multiplication of cyclic frequency, \( f \), and internal energy change, \( \Delta U \). Substituting equation 13D into equation 14A, we can express the volumetric power dissipation, \( P \), as:

\[
P = \frac{2\mu_0 H_0^2 (f \pi)^2 \chi'_o(T)}{1 + (2\pi f \tau)^2} \quad (14B)
\]

Finally, to obtain the modified power dissipation for magnetic nanoparticle aggregates, we substituted equation 12 for \( \chi'_o(T) \) into equation 14B:

\[
P = \frac{2\mu_0 H_0^2 (f \pi)^2}{1 + (2\pi f \tau)^2} \left[ M_{\varphi} \left( \frac{T}{T^*} \right) L \left( \frac{\mu_o m H_o}{k_B T} \right) + M_{\sigma} \left( 1 - \frac{T}{T^*} \right) \frac{1}{2} L \left( \frac{\mu_o m H_o}{k_B T} \right) \right] \quad (14C)
\]
Specific loss power

The SLP can be calculated as:

\[
\text{SLP} = \frac{P}{\rho \phi}
\]  

(15A)

where \(\rho\) denotes the mass density of the ferrofluid. The corresponding adjusted SLP accounting for cluster formation in the ferrofluid can then be expressed as:

\[
\text{SLP} = \frac{2\mu_r H_0 (\pi f)^2}{\rho [1 + (2\pi f \tau)^2]} \left[ M_{\text{dm}} \left( \frac{T}{T^w} \right) L \left( \frac{\mu_0 m H_0}{k_b T} \right) 
+ M_{\phi} \left( 1 - \frac{T}{T^w} \right)^{\frac{1}{2}} L \left( \frac{\mu_0 m H_0}{k_b T} \right) \right]
\]  

(15B)

Comparison with experimental results

To determine the validity and accuracy of our revised cluster-based model, predicted SLP values based on the revised cluster-based model and the Rosensweig model were compared with available experimental results using magnetite Fe\(_3\)O\(_4\) magnetic nanoparticles and in Table 2 for cobalt ferrite CoFe\(_2\)O\(_4\) magnetic nanoparticles.

In vivo demonstration of magnetic nanoparticle aggregation in cancer tissues

In order to demonstrate the aggregation of magnetic nanoparticles in biomedical applications, we inspected MR T\(_2\)-weighted imaging and the pathological iron stain of pancreatic cancers in in vivo xenograft mouse models, which were targeted and labeled by magnetic nanoparticles. To enhance targeting specificity and efficiency, anti-cancer-antigen 19-9 (anti-CA 19-9) antibodies (400 \(\mu\)g) were conjugated to NH\(_2\)-PEG-coated magnetic nanoparticles (5 mg) utilizing reductive amination chemistry into a 900 \(\mu\)L solution. Conjugation was verified using dynamic light scattering for particle size determination and the Bradford protein assay. More details on the preparation, bioconjugation, and characterization of the anti-CA 19-9 antibodies–magnetic nanoparticles can be found in the “Supplementary Materials”.

The human pancreatic cancer cell line, BxPC-3, which reveals positive expression of CA19-9 antigen,\(^{32}\) was

<table>
<thead>
<tr>
<th>Magnetic nanoparticle</th>
<th>Magnetite Fe(_3)O(_4)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Magnetic anisotropy constant, (K_a) (kJ/m(^3))</td>
<td>21</td>
</tr>
<tr>
<td>Domain magnetization of monomers, (M_{\text{dm}}) (kA/m)</td>
<td>446</td>
</tr>
<tr>
<td>Viscosity of the carrier fluid, (\eta) (kg/m/s)</td>
<td>0.0007 (water)</td>
</tr>
<tr>
<td>Temperature, (T) (K)</td>
<td>300</td>
</tr>
<tr>
<td>Critical temperature, (T^w) (K)</td>
<td>358</td>
</tr>
<tr>
<td>Alternating magnetic field</td>
<td></td>
</tr>
<tr>
<td>Frequency, (f) (kHz)</td>
<td>80</td>
</tr>
<tr>
<td>Amplitude, (H_0) (kA/m)</td>
<td>32.5</td>
</tr>
<tr>
<td>Magnetic nanoparticle mean diameter (nm)</td>
<td>7.5</td>
</tr>
<tr>
<td>SLP (W/g)</td>
<td></td>
</tr>
<tr>
<td>Experiment(^{22,23})</td>
<td>15.6</td>
</tr>
<tr>
<td>Cluster-based model</td>
<td>0.13</td>
</tr>
<tr>
<td>Rosensweig model</td>
<td>0.11</td>
</tr>
<tr>
<td>Reference</td>
<td>Ma et al(^{22})</td>
</tr>
<tr>
<td>Figure number</td>
<td>Figure 3</td>
</tr>
</tbody>
</table>

Abbreviation: SLP, specific loss power.
Table 2  Experimental results and parameters used in the theoretical calculations of the SLP for cobalt ferrite CoFe$_2$O$_4$ magnetic nanoparticles, to determine the validity and accuracy of the revised cluster-based model, as shown in Figures 5 and 6

<table>
<thead>
<tr>
<th>Magnetic nanoparticle</th>
<th>Cobalt ferrite CoFe$_2$O$_4$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Magnetic anisotropy constant, $K_a$ (kJ/m$^3$)</td>
<td>1,200</td>
</tr>
<tr>
<td>Domain magnetization of monomers, $M_{sat}$ (kA/m)</td>
<td>425</td>
</tr>
<tr>
<td>Viscosity of the carrier fluid, $\eta$ (kg/m/s)</td>
<td>0.0007 (water)</td>
</tr>
<tr>
<td>Temperature, $T$ (K)</td>
<td>300</td>
</tr>
<tr>
<td>Critical temperature, $T^*$ (K)</td>
<td>358</td>
</tr>
<tr>
<td>Alternating magnetic field</td>
<td></td>
</tr>
<tr>
<td>Frequency, $f$ (kHz)</td>
<td>167</td>
</tr>
<tr>
<td>Amplitude, $H_{ac}$ (kA/m)</td>
<td>21</td>
</tr>
<tr>
<td>Magnetic nanoparticle size</td>
<td></td>
</tr>
<tr>
<td>Mean diameter (nm)</td>
<td>5.5, 5.9, 6.0, 6.2, 6.7, 3.9, 9.1</td>
</tr>
<tr>
<td>Standard deviation, $\sigma$</td>
<td>0.19, 0.18, 0.19, 0.23, 0.21, 0.40, 0.22</td>
</tr>
<tr>
<td>SLP (W/g)</td>
<td>76.7, 105, 153, 188, 250, 40, 360</td>
</tr>
<tr>
<td>Experiment$^{24,25}$</td>
<td></td>
</tr>
<tr>
<td>Cluster-based model</td>
<td>140, 183, 199, 235, 294, 33.1, 361</td>
</tr>
<tr>
<td>Rosensweig model</td>
<td>151, 198, 215, 255, 318, 35.8, 387</td>
</tr>
<tr>
<td>Reference</td>
<td>Baldi et al$^{24}$, Fortin et al$^{25}$</td>
</tr>
<tr>
<td>Figure number</td>
<td>Figure 5, Figure 6</td>
</tr>
</tbody>
</table>

Abbreviation: SLP, specific loss power.

The MRI experiments were performed on Varian INOVA 7-T micro-imaging spectrometer (Varian Inc., Walnut Creek, CA, USA) at day 35 after tumor implantation. The multiple slice spin-echo $T_2$-weighted images were acquired on the axial plane with TR = 7.5 s, TE = 10 ms, 30 ms, 50 ms, FOV = 32×32 mm, thickness = 0.5 mm, pixel size = 128×128, number of slices = 64, and number of scans = 1. Prior to injecting 200 L CA19-9-magnetic nanoparticle (corresponding to 2.0 mg Fe/Kg mouse) to the tail vein of the mouse, we injected 100 g IgG (Immunoglobulin G, Sigma-Aldrich) to the tail vein of the mouse to suppress the immune response of the mouse. Administration of IgG to mice in combination with particulate antigen suppressed the immune response that was mediated by macromolecules found in extracellular fluids such as secreted antibodies, complement proteins, and certain antimicrobial peptides by masking B-cell epitopes.$^{33}$

Results and discussion

In vivo demonstration of magnetic nanoparticle aggregation in pancreatic cancers

Pancreatic cancer, called the silent killer, is the fourth leading cause of cancer-related death in both men and women in the USA. Due to difficulties in diagnosis and therapy, pancreatic cancer patients’ 5-year survival rate is only about 1% in the USA. Nonetheless, hope for mitigating...
pancreatic cancers arises from the early detection and targeted thermo-chemotherapy through MR nano-theranostics. Figure 1 demonstrates the formation of magnetic nanoparticle aggregates in targeted pancreatic cancers, which motivated the authors to propose a revised cluster-based model to more accurately predict SLP and to optimize heating efficiency for future in vivo applications of MR nano-theranostic hyperthermia in cancer therapy.

Comparison with the Rosensweig model

To investigate how the aggregation behavior of interacting magnetic nanoparticles affects the hyperthermia properties, the SLP was computed from the revised cluster-based model and then was compared with that from the original Rosensweig model. Because SLP is proportional to the volumetric power dissipation, which is, in part, determined by the imaginary part of the magnetic susceptibility as described in equations 14A and 15A, changes in the imaginary part of the magnetic susceptibility due to magnetic nanoparticle aggregation would be reflected on the resulting SLP. Experimental results reported by Hergt et al regarding the relationship between the frequency, \( f \), and the imaginary part of the magnetic susceptibility of the ferrofluid, \( \chi'' \), were shown to be significantly different from the predicted Rosensweig theoretical values. Specifically, experimental results for the colloidal-based ferrofluid suspension were shown to have a lower magnetic susceptibility peak value than predicted, implying the model suggested by Rosensweig alone cannot fully characterize the
ferrofluid system. Our revised cluster-based model aims to explain the inconsistency between the original Rosensweig prediction and experimental results by considering cluster formation in the ferrofluid solution.

Using the experimental parameters previously reported by Hergt et al., we compared the differences between the Rosensweig model and the revised cluster-based model, as shown in Figure 2. The imaginary part of the magnetic susceptibility, $\chi''$, was calculated as a function of the alternating magnetic field frequency, $f$, for magnetic nanoparticle diameter $d = 18$ nm, alternating magnetic field amplitude $H_0 = 11$ kA/m, and magnetic anisotropy constant $K_a = 15$ kJ/m$^3$. $\chi''$ as a function of the magnetic nanoparticle diameter for alternating magnetic field frequency $f = 410$ kHz, alternating magnetic field amplitude $H_0 = 11$ kA/m, and magnetic anisotropy constant $K_a = 15$ kJ/m$^3$. The SLP, as a function of the magnetic nanoparticle diameter, using the same parameters as those in (B).

**Figure 2** Comparison with the Rosensweig model.

**Notes:** The imaginary part of the magnetic susceptibility, $\chi''$, and the SLP were computed by our revised cluster-based model (red solid line) and the Rosensweig model (blue dashed line). (A) $\chi''$ as a function of the alternating magnetic field frequency, $f$, for magnetic nanoparticle diameter $d = 18$ nm, alternating magnetic field amplitude $H_0 = 11$ kA/m, and magnetic anisotropy constant $K_a = 15$ kJ/m$^3$. (B) $\chi''$ as a function of the magnetic nanoparticle diameter for alternating magnetic field frequency $f = 410$ kHz, alternating magnetic field amplitude $H_0 = 11$ kA/m, and magnetic anisotropy constant $K_a = 15$ kJ/m$^3$. (C) The SLP, as a function of the magnetic nanoparticle diameter, using the same parameters as those in (B).

**Abbreviation:** SLP, specific loss power.

nanoparticle aggregation increases the overall cluster magnetic anisotropy ($K_a$), as described in equation 5B, and decreases both the domain magnetization ($M_d$) and the average magnetic moment ($\bar{m}$) of clusters due to the minimization of internal energy, as shown in equation 8. Particularly, the increase in cluster magnetic anisotropy is reflected in the effective relaxation time constant, $\tau$, by affecting the Neel relaxation time constant, $\tau_N$, as denoted in equations 3 and 4, while the decrease in both the domain magnetization and the average magnetic moment of the clusters is reflected in the equilibrium magnetic susceptibility, as shown in equation 12. These factors altogether contribute to the shift of the curve of $\chi''$, resulting in the shifted theoretical SLP value, as shown in equation 15B. Therefore, the theoretical SLP based on equation 15B was plotted in Figure 2C as a function of the magnetic nanoparticle diameter using the same parameters as those in Figure 2B. The predicted SLP values reflect the variation in the imaginary part of the magnetic susceptibility, as these two parameters are linearly related to each other (equation 14A).
The main difference between the revised cluster-based model and the Rosensweig model is the consideration of magnetic nanoparticle interactions within the real ferrofluid. Because the Rosensweig model assumes that magnetic nanoparticles act as individual units independent of each other, the SLP value, as well as the optimal magnetic nanoparticle size, is overestimated. In biomedical applications, however, magnetic nanoparticles are not found simply in single units, but rather as aggregated clusters (Figure 1). Accurate theoretical models should, therefore, reflect the fraction of clusters in the real ferrofluid. By taking cluster formation into consideration, the revised cluster-based model predicts SLP values and the corresponding optimal magnetic nanoparticle diameter at the maximum SLP to be about 20%–25% smaller than those made by the Rosensweig model, as shown in Figure 2C.

Comparison with the experimental results of magnetite $\text{Fe}_3\text{O}_4$ magnetic nanoparticles

SLP were computed based on the revised cluster-based model and the Rosensweig model and then were compared with the experimental results of magnetite $\text{Fe}_3\text{O}_4$ magnetic nanoparticles reported by Ma et al$^{22}$ and Lartigue et al$^{23}$ as summarized in Table 1 and shown in Figures 3 and 4. Magnetite $\text{Fe}_3\text{O}_4$ is the most popular form of magnetic nanoparticles, as it is well tolerated by the human body. Although there are still some differences between our cluster-based prediction and the experimental results, our model offers relatively more accurate estimates of SLP in comparison with the Rosensweig model. Within the superparamagnetic size range (i.e. magnetic nanoparticle diameter 5–50 nm), the SLP values increase significantly with the increase of the nanoparticle size, mainly due to the onset of other heat generation mechanisms.$^{10,13}$ However, aggregation of magnetic nanoparticle shifts the overall curve to the left (i.e. smaller magnetic nanoparticle diameter), predicting lower SLP values when compared with the predictions made by the Rosensweig model, in agreement with Figure 2. Notably, the revised cluster-based model works especially well within the magnetic nanoparticle diameter range of 10–20 nm, which is commonly chosen for MR nano-theranostics. On the other hand, neither theoretical model accurately predicts the SLP for magnetic nanoparticles with a diameter >20 nm (Figure 4). This divergence can be attributed to the availability of other heat generation mechanisms and nonlinear effect, such as hysteresis,$^{10,13}$ associated with larger magnetic nanoparticle diameters.

Comparison with the experimental results of cobalt ferrite $\text{CoFe}_2\text{O}_4$ magnetic nanoparticles

Additional comparisons were made using experimental results of cobalt ferrite $\text{CoFe}_2\text{O}_4$ reported by Baldi et al$^{24}$
magnetic anisotropy constant in the theoretical calculations are summarized in Table 2: cobalt ferrite CoFe$_2$O$_4$ model (blue dashed line), using the experimental results and parameters reported by Baldi et al$^{40}$ (black filled circle). The experimental results and the parameters used in the theoretical calculations are summarized in Table 2: cobalt ferrite CoFe$_2$O$_4$, magnetic anisotropy constant $K_a=1,200$ kJ/m$^2$, domain magnetization of monomers $M_u=425$ kA/m, alternating magnetic field frequency $f=167$ kHz, alternating magnetic field amplitude $H_0=21$ kA/m, viscosity of the carrier fluid (water) $\eta=0.0007$ kg/m/s, temperature $T=300$ K, critical temperature $T^c=358$ K, and the mean (standard deviation $\sigma$) of the magnetic nanoparticle diameter $=6.7$ nm ($\sigma=0.23$ nm).

**Abbreviation:** SLP, specific loss power.

and Fortin et al$^{33}$ as summarized in Table 2 and shown in Figures 5 and 6, respectively. Similar to the previous comparison with the experimental results of magnetite Fe$_3$O$_4$ magnetic nanoparticles, the revised cluster-based model approaches the experimental results better than the Rosensweig model, as the maximum and overall SLP is reduced by the aggregation of magnetic nanoparticles. Again, SLP of magnetic nanoparticles with diameters between 10 and 20 nm was more accurately predicted by the revised cluster-based model. However, since cobalt ferrite CoFe$_2$O$_4$ possesses a relatively larger magnetic anisotropy constant than magnetite Fe$_3$O$_4$, the effect of aggregation on magnetic anisotropy becomes less significant, resulting in a smaller shift to the left (i.e. smaller magnetic nanoparticle diameter) by the revised cluster-based model, as portrayed in both Figures 5 and 6.

**Conclusion**

MR nano-theranostic hyperthermia uses nontoxic, biocompatible magnetic nanoparticles to target and accumulate at the lesions to generate enhanced contrast for early lesion detection and generate heat to kill lesion cells directly through hyperthermia or indirectly through thermal activation and control releasing of drugs.$^{34-38}$ By considering the effects of magnetic nanoparticle aggregation on MR nano-theranostic hyperthermia, our revised cluster-based model provides a more accurate prediction of experimental values, as shown in Figures 3–6 for magnetite Fe$_3$O$_4$ and cobalt ferrite CoFe$_2$O$_4$ magnetic nanoparticles. The aggregation of magnetic nanoparticles increases the cluster magnetic anisotropy while reducing both the cluster domain magnetization and the average magnetic moment, which, in turn, decreases the imaginary part of the magnetic susceptibility to shift the predicted SLP toward smaller magnetic nanoparticle diameter with lower peak values. The effect of magnetic nanoparticle aggregation can also be understood in terms of energy transfer. A portion of the energy provided by the magnetic field is absorbed by the magnetic nanoparticle aggregates to overcome inter-nanoparticle interactions, such as electrostatic attraction, electrostatic repulsion, steric repulsion, and magnetic dipolar interactions to disrupt the aggregates into monomers. As a result, the heating efficiency is decreased and the SLP values are less than the prediction made by the Rosensweig theory.

The improvement in the prediction accuracy provided by the revised cluster-based model is particularly pronounced when the magnetic nanoparticle diameter is in the range of $\sim$10–20 nm or, equivalently, the resulting drug–nanoparticle–ligand conjugates in the range of $\sim$30–50 nm. This happens to be an important size range for MR nano-theranostics, as recent studies showed that anticancer nano-medicine with 50-nm nanoparticle size provides the optimal combination of deep tumor tissue penetration, efficient cancer cell internalization,
and slow tumor clearance, and therefore exhibits the highest efficacy against both primary and metastatic tumors in vivo.39

When the magnetic nanoparticle becomes larger, as seen in the case of magnetite Fe3O4 in Figure 4, the prediction becomes inaccurate even with the revised cluster-based model, mainly due to alternative heat generation mechanisms and nonlinear response of magnetic susceptibility,40–42 which motivates more sophisticated and accurate theoretical models in the future.

Finally, nanoparticle size plays a pivotal role in nano-theranostics, as it determines their biodistribution, tumor penetration, cellular internalization, clearance from blood plasma and tissues, as well as excretion from the body—all of which impact the overall therapeutic efficacy against cancers.39,43 Our studies show that, as far as MR nano-theranostic hyperthermia is concerned, a relatively 20%–25% smaller magnetic nanoparticle diameter should be chosen to reach the maximal heating efficiency in comparison with the optimal size predicted by previous models.

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Disclosure

The authors report no conflicts of interest in this work.

References


Supplementary materials
Orthotopic pancreatic cancer mouse models

The 4-week-old male BALB/c nude mice (N=4) were obtained from BioLASCO, Taipei, Taiwan. BALB/c is an albino, laboratory-bred strain of the house mouse from which a number of common substrains are derived. BALB/c mice are distributed globally and are among the most widely used inbred strains used in animal experimentation.

Orthotopic pancreatic cancer mouse models are preferred in this work, because they offer tissue site-specific pathology, allow studies of metastasis, and are generally deemed more clinically relevant. Orthotopic implantation of pancreatic cancer cells includes the following steps: 1) Make incision with sterile microscissors beside the splenic silhouette. 2) Expose the entire pancreas and spleen by using a pair of blunt-nose forceps. 3) Insert the needle with the human pancreatic cancer cells into the tail of the pancreas and pass into the pancreatic head area. Suture the abdominal muscle layer first as putting back the pancreas and spleen into the abdominal cavity and close the skin.

We waited until the volume of the subcutaneous xenograft pancreatic cancer reached 5 mm³. We first injected 100 g IgG (Immunoglobulin G) from the tail vein of the mouse to suppress the immune response of the mouse. Then we injected 200 L CA19-9-magneic nanoparticle (corresponding to 2.0 mg Fe/kg mouse) from the tail vein of the mouse. All injections were performed under anesthesia by isoflurane (Panion & BF Biotech Inc., Taipei, Taiwan), and all efforts were made to minimize suffering.

During the MRI acquisition, mice were anesthetized by inhalation of isoflurane (Panion & BF Biotech Inc.). A vaporizer specially calibrated for isoflurane was used to accurately control the anesthetic concentration during MRI scanning. The physiological status of the mice was kept under surveillance with a small animal monitoring system (SA Instruments Stony Brook, NY, USA). Mice were humanely sacrificed after experiments. All animal procedures were in accordance with the regulations approved by the Institution Animal Care and Utilization Committee at National Taiwan University (approval number NTU-103-EL-61).

Tissues were fixed in 10% formalin overnight, embedded in paraffin, and then sectioned. Tissues sections with a thickness of 5 μm were deparaffinized in xylene, rehydrated in a gradient ethanol series, and incubated in blocking buffer. To visualize nuclei and cytoplasm, H&E staining was performed according to the standard protocols. Images of the tissues were acquired using a wide-field scanner with a 40x objective and detected with a color microscope camera (DFC7000T, Leica, Wetzlar, Germany).

To visualize the magnetic nanoparticle aggregates, Prussian blue staining was performed according to the standard protocols. The staining is an optical method based on the binding of cellular ferric ions to the soluble ferrocyanide salt at low pH, forming an insoluble deep blue hydrated ferric ferrocyanide complex (i.e. Prussian blue dye). Therefore, in order to detect magnetic nanoparticle aggregates in tissue sections, the specimens were deparaffinized and treated with 20% aqueous solution of concentrated HCl to dissolve the magnetic nanoparticles to release ferric iron in the cells.

Preparation, bioconjugation, and characterization of the anti-CA 19-9 antibodies—magnetic nanoparticles

To oxidize the glycosylated anti-CA 19-9 antibodies, 400 μg of the antibody was mixed with 40 μL of 0.10 M sodium periodate solution and reacted for 45 min in dark at room temperature. Then 40 μL of 0.20 M Na₂SO₄ solution was immediately added into the mixture and allowed to react for another 10 min. The sample was then run through D-Salt Dextran Desalting Columns (Thermo Fisher Scientific, Waltham, MA, USA) to isolate the oxidized antibody from the mixture.

The oxidized antibody was quickly mixed with the amine-coated magnetic nanoparticles (0.054 nmole/mL) (Ocean Nanotech, Springdale, AR, USA) at a pH of 8.0 to reduce aggregation and maximize Schiff base formation while preventing the denaturation of the antibody. The reaction was then shaken at room temperature for 6 h. To stabilize the Schiff bases, 53 μL of 5.0 M sodium cyanoborohydride solution was added and reacted for 45 min to reduce the bond to a secondary amine linkage. Additionally, 268 μL of 1.0 M ethanolamine solution was added to the mixture to quench the unreacted aldehyde groups on the antibody. This reaction mixture was then purified by washing 5 times using Amicon Ultra Centrifugal Filters (Millipore, Carrigtwohill, Ireland) to remove the quenching reagents. Unbound antibody was also purified from conjugated magnetic nanoparticles through a separation magnet (Ocean Nanotech) overnight. The final solution was suspended in PBS at a concentration of 5 mg Fe/mL.

Dynamic light scattering (DLS) measurements were taken to verify the bioconjugation between the anti-CA
19-9 antibodies and the magnetic nanoparticles. DLS measurements were taken on a Zetasizer Nano using a disposable, low-volume cuvette. The standard protein method on the detector was utilized to generate a size distribution plot. The diameter of unconjugated magnetic nanoparticles was measured to be 25 nm, while that of the conjugated magnetic nanoparticles was 38 nm, as shown in Figure S1.

**Figure S1** Dynamic light scattering measurements were taken to verify the bioconjugation between the anti-CA 19-9 antibodies and the magnetic nanoparticles. **Notes:** The standard protein method on the detector was utilized to generate a size distribution plot. The diameter of unconjugated magnetic nanoparticles was measured to be 25 nm, while that of the bioconjugated magnetic nanoparticles was 38 nm. **Abbreviation:** anti-CA, anti-cancer-antigen.