Dispersion relations of cytoskeleton dynamics

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Abstract: While it is well known that the cytoskeleton plays a fundamental role in maintaining cell shape, performing cell division, and intracellular transport, its spatiotemporal dynamics are insufficiently understood. The dispersion relation, which is fundamental for understanding the connection between spatial and temporal scales of a dynamic system, was employed here for the first time to study the activity of actin and microtubules. Using green fluorescence protein for time-lapse imaging of the cytoskeleton, we showed that the dispersion relation can distinguish between diffusive and active transport of actin and microtubule filaments. Our analysis revealed that along the filaments, the transport was deterministic, as one might expect as the result of the active polymerization process, while across the filaments diffusion was dominant. Furthermore, using drugs to block the polymerization–depolymerization of both actin and microtubules, we measured that the transport immediately became diffusive, as expected. However, unexpectedly, our results indicated that within a few minutes from blocking its polymerization, actin recovered an active transport component. This deterministic component vanished upon treatment with nocodazole, indicating that fragments of actin were actively transported along microtubules. Because it provides information over broad temporal and spatial scales, this approach promises to provide a new window into the active processes associated with live cells.

Keywords: quantitative phase imaging, QPI, spatial light interference microscopy, SLIM, microtubule dynamics, actin dynamics

Introduction

Mass transport along actin and microtubules within the live cell plays a crucial role in regulating cell function, from cell differentiation and motility to mitosis and apoptosis.1 Studying cytoskeletal dynamics is extremely interesting not only at the basic science level but also at the clinical level, as it may open new avenues for the treatment of important disease.2 For example, disruption of cargo transport along neural processes can lead to neurodegenerative diseases, such as Alzheimer’s disease.3,4

Despite great progress on the subject, the role of the cytoskeleton in intracellular transport remains insufficiently understood.5–7 Trafficking at the intracellular level results from both thermal diffusion and the activity of molecular motors.8 This process has been examined through techniques that generally rely on fluorescence imaging,9 eg, fluorescence speckle microscopy,10 fluorescence correlation spectroscopy,11 Förster resonance energy transfer,12 fluorescence recovery after photobleaching,13 and fluorescence lifetime imaging microscopy.14 Recently, there has been significant progress...
in superlocalization microscopy, such as stochastic optical reconstruction microscopy,¹⁵ photoactivated localization microscopy,¹⁶,¹⁷ and their precursor, fluorescence imaging with 1 nm accuracy,¹⁸ which are closing the gap between cellular- and molecular-scale biology. In combination with fluorescence microscopy, particle tracking is a widely used approach for studying the transport of discrete objects inside the cell, such as embedded particles, organelles, and vesicles.¹⁹-²² Analyzing the trajectories of these particles in terms of their mean squared displacements provides valuable information about the nature of transport and even the rheology of the surrounding medium. However, this approach has limited applicability when the system of interest is continuous, such as actin and microtubule cytoskeletons at spatial scales larger than the mesh size. Furthermore, particle tracking does not contain explicit spatial information.

In order to meet this experimental challenge of investigating mass transport in live cells over broad spatiotemporal scales, recently we proposed a new approach, referred to as dispersion-relation fluorescence spectroscopy (DFS).²³ This method analyzes the full-field fluorescence images in a time lapse and provides the dispersion relation associated with the dynamic transport. This dispersion relation is in the form of a power law \(-Γ(q) = q^{-α}\) which describes the relaxation rate (in rad/s) of the spatial mode \(q\) (in μm/s). Physically, \(1/Γ\) describes the correlation time associated with a spatial disturbance of wavelength \(1/q\). Importantly, the dispersion curve allows us to distinguish between diffusion and directed transport and their specific spatiotemporal scales.

In our study, we used time-lapse imaging of green fluorescence protein (GFP) fused to actin and microtubules to study their spatiotemporal fluctuations. We found that DFS is capable of revealing subtle changes in the cytoskeleton dynamics associated with the integrity of the polymerization process. Specifically, we demonstrated that DFS can quantitatively monitor the transition from deterministic to random transport when the polymerization of the cytoskeleton is blocked. Our study suggested that cells may have an interesting mechanism for active transport of actin along microtubules.

**Materials and methods**

**Cell culture**

Mouse embryonic fibroblasts (MEFs) were obtained from American Type Culture Collection (Manassas, VA, USA). These cells were cultured in a 37°C incubator with humid atmosphere, 5% CO₂, and 95% air, and were grown in Dulbecco’s modified Eagle’s medium supplemented with 100 μg/mL ampicillin, 100 μg/mL streptomycin, 2 g/L sodium bicarbonate, and 10% fetal bovine serum (FBS). The cells were cultured in a 13 mm glass-bottom dishes, which were placed in a 5% CO₂-1% air, and were grown in an atmosphere of 5% CO₂-1% air, and were grown in American Type Culture Collection (Manassas, VA, USA). Mouse embryonic fibroblasts (MEFs) were obtained from Cell culture Materials and methods study suggested that cells may have an interesting mechanism when the polymerization of the cytoskeleton is blocked. Our method analyzes the full-field fluorescence images in a time lapse and provides the dispersion relation associated with the dynamic transport. This dispersion relation is in the form of a power law \(-Γ(q) = q^{-α}\) which describes the relaxation rate (in rad/s) of the spatial mode \(q\) (in μm/s). Physically, \(1/Γ\) describes the correlation time associated with a spatial disturbance of wavelength \(1/q\). Importantly, the dispersion curve allows us to distinguish between diffusion and directed transport and their specific spatiotemporal scales.

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**Results**

We used DFS to study actin dynamics under the effect of cyto-D. GFP-fused actin of MEF cells was imaged continuously using epifluorescence (see the Materials and methods section for details on GFP transfection and imaging). Time-lapse images were acquired over 4.25 minutes at an acquisition rate of 1 frame/second. The results of the first experiment are summarized in Figure 1. Individual images of normal cells revealed the actin bundles oriented along certain directions, as illustrated in Figure 1A. Consequently, the dispersion map (Figure 1D) was also anisotropic, indicating that transport along the bundles was significantly different than that across them. Interestingly, along the filament bundles, DFS revealed deterministic transport, as indicated by the linear dependence of the \(Γ vs q\) curve (black squares in Figure 1G). By contrast, the dynamics across the actin filaments were diffusive – \(Γ ∝ q^2\).
the transport along the filaments returned to deterministic behavior (red triangles in Figure 1G).

These experiments demonstrate that the active transport is strongly dependent on the integrity of the actin filaments. At the same time, DFS appears to be a valuable tool for studying such dynamics, where particle-tracking methods are limited. Note that at high \( q \)-values, the curves in Figure 1G deviate from the power laws of \( q^2 \) and \( q^3 \) and level off. This is because of the finite acquisition rate of our measurement, which set the maximum \( F \)-value. The \( q^2 \) curves level at lower \( q \)-values were due to the faster transport process.

Next, we tested the sensitivity of DFS to microtubule dynamics. We performed experiments on GFP-labeled microtubules of MEFs under normal and nocodazole-treatment conditions (Figure 2). The fluorescence images were taken

This result suggests that the continuous polymerization process at the end of the actin filaments was an active process governed by ATP consumption rather than thermal noise. In order to test this hypothesis, we imaged the same cells after adding cyto-D, which blocks the polymerization process. Clearly, cyto-D destroyed the actin filamentous structure, as evidenced by Figure 1B. As a result of crumbling the filaments, the dispersion map became isotropic (Figure 1E).

More importantly, the dispersion relation indicated a clear \( q^2 \) behavior, and thus Brownian transport (blue circles in Figure 1G). Further, as a control experiment, we washed out the cyto-D using culture medium and incubated the cells at 37°C and 5% CO\(_2\) for 1 hour. After the washout, the actin structure partially recovered (Figure 1C), and remarkably

**Figure 1** Short-term effect of cyto-D treatment on MEFs.

**Notes:** (A) Actin-GFP image of a transfected MEF cell. (B) The same cell imaged after cyto-D was added to the cell dish. (C) The same cell imaged after the cyto-D was washed out. After 2 hours, the actin-filament structure gradually recovered. (D–F) Dispersion maps of \( \gamma(q, q) \) associated with the time-lapse images in A–C. (G) The dispersion curves along fiber directions (red line in A) were plotted on the same graph. The black squares represent the normal MEF shown in A, and exhibit linear dependence (directed transport). The green line is a linear curve indicating deterministic transport. The blue circles correspond to B, where the cells were treated with cyto-D, and exhibit a quadratic dependence (diffusion). The red triangles represent the cell in C, recovered after washing out cyto-D. Note that the normal and recovered cells exhibit an identical dispersion relation, which indicates that the dynamics were fully recovered as a result of washout. All time-lapse images were acquired at 1 frame/second for 4.25 minutes using epifluorescence microscopy.

**Abbreviations:** MEF, mouse embryonic fibroblast; cyto-D, cytochalasin D; GFP, green fluorescence protein.

**Figure 2** Short-term effect of nocodazole treatment on MEFs.

**Notes:** (A) Tubulin-GFP image of a transfected MEF cell. (B) The same cell imaged after nocodazole was added to the cell dish. (C) The same cell imaged after the nocodazole was washed out. (D–F) Dispersion maps of \( \gamma(q, q) \) associated with the time-lapse images in A–C. (G) The dispersion curves along fiber directions (red line in A) were plotted on the same graph. The black squares represent the normal MEF shown in A, and exhibit linear dependence (directed transport). The blue circles correspond to B, where the cells were treated with nocodazole, causing the curve to flatten out. The red triangles are associated with the cell in panel C, which recovered after washing out the nocodazole. The green lines indicate the theoretical fit for the \( q \) and \( q^2 \) dependence. Note that the normal and recovered cells exhibit an identical dispersion relation, which indicates that the dynamics were fully recovered as a result of washout. All time-lapse images were acquired at 1 frame/second for 4.25 minutes using epifluorescence microscopy. \( q \) corresponds to diffusion.

**Abbreviations:** MEF, mouse embryonic fibroblast; cyto-D, cytochalasin D; GFP, green fluorescence protein.
with the same acquisition rate, 1 frame/second, for 4.25 minutes. Figure 2A and D show the image and DFS map, respectively, of a normal MEF with its microtubules labeled by GFP. The dispersion curve (Figure 2G) indicates that the transport along microtubule filaments was directed ($I = q$). The same cell is shown in Figure 2B after nocodazole was added to the cell petri dish to depolymerize the microtubules. Interestingly, while the image itself is not informative about the microtubule-polymerization state, the DFS map, ie, Figure 2E, reveals significant changes from its normal counterpart, shown in Figure 2D. Due to the nocodazole, the DFS map became narrower and isotropic. This transition from anisotropy to isotropy indicates that the microtubules were characterized by polarity, which plays a role in intracellular transport. The effect is further illustrated in Figure 2G, where profiles along the direction indicated in Figure 2A are presented. Note that after addition of the drug, the dispersion curve flattened (blue-circle curve). Again, we performed a control experiment where we washed out the drug with fresh medium and kept the cells at 37°C and 5% CO$_2$ for approximately an hour. This washout procedure partially recovered the filament structure. After the washout, the dispersion curve (red triangles in Figure 2G) overlapped perfectly with the one before treatment (black square), indicating that the microtubule active dynamics also recovered.

Next, we studied in more detail the effect of the two drugs as it developed in time. Figure 3 illustrates the gradual effect of nocodazole used to block the microtubule polymerization. In order to monitor this highly dynamic process, we recorded time-lapse image sets at intervals of 20 minutes. Each fluorescence-data set (Figure 3A–D) was taken at the same acquisition rate of 1 frame/second over 4.25 minutes. It can be seen that due to nocodazole, the DFS maps gradually became isotropic (Figure 3E–H). The dispersion relation was analyzed along two particular directions, marked by the black and red lines in Figure 3E–H; the azimuthal average is also shown. These dispersion curves consistently flattened out after the polymerization of tubulin was disrupted by nocodazole, as shown in Figure 3I–L. As the microtubule filaments were broken down, the resulting monomers were smaller in size and thus moved faster in the solution. Since our acquisition rate and therefore maximum $I$ was constant, the effect of the drug was to gradually level off the DFS curves. We expected that transport would become diffusive upon filament depolymerization.

![Figure 3](image-url) Long-term effect of nocodazole treatment on MEFs. Notes: (A) Tubulin-GFP image of a transfected MEF cell. (B–D) The same cell at different points in time, as indicated, after adding nocodazole. (E–H) Dispersion maps of $I(q, q_i)$ associated with images A–D, with two axes of symmetry shown. (I–L) Dispersion-relation curves plotted along the two axes ($\theta_1$, $\theta_2$), and azimuthally averaged, as indicated. The green lines are linear curves indicating deterministic transport. Before treatment, the linear dependence (deterministic motion) was dominant. Under nocodazole treatment, the curves flatten out progressively. All time-lapse images were acquired at 1 frame/second for 4.25 minutes using epifluorescence microscopy. $q_i$ corresponds to deterministic transport. Abbreviation: MEF, mouse embryonic fibroblast; GFP, green fluorescence protein; T, time.
Nocodazole-treated tubulin did not show this $q^2$ curve, only because its motion was faster than the acquisition rate. Note the highest value of $\Gamma$ was limited by the frame rate, and the lowest $\Gamma$-value was due to the total acquisition time.

We performed an analog experiment to study the effect of the cyto-D on actin. The results are summarized in Figure 4 and reveal an unexpected behavior, as follows. Immediately after the addition of cyto-D (Figure 4B), not surprisingly, the actin-filament transport transitioned from a combination of directed and diffusive motions (Figure 4I) to a largely diffusive motion (Figure 4J). However, after approximately 20 minutes, the data indicated directed transport again, as illustrated by the $q^1$ dependence in Figure 4K. Imaging the cell over a longer period of time did not reveal a tendency to return to diffusion. This result was unexpected. We hypothesize that this effect was due to the actin fragments that became attached to the microtubules and thus were subjected to active transport. Results from these experiments are summarized in Figure 5.

In order to prove this hypothesis, we ran a double-treatment test, ie, after the actin polymerization was blocked with cyto-D (Figure 5B and C), the microtubule polymerization was further disrupted with nocodazole (Figure 5D–F). Therefore, following cyto-D-induced transition from directed motion, ($q^1$ in Figure 5N) to diffusive transport ($q^2$ in Figure 5O) and directed again ($q^1$ in Figure 5P), the actin-filament transport eventually became purely diffusive ($q^2$ in Figure 5Q and R) after the addition of nocodazole. The viability of cells was confirmed by the reversibility of both structure and function after the drug washout. These results show that along with the microtubule-structure dissociation, the actin fragments eventually dissolved in the cytoplasm and underwent random motion, thus proving our hypothesis.

**Discussion**

Aberrant cytoskeleton dynamics have been established to reflect the cellular characteristics of various diseases. As such, the knowledge about cytoskeleton dynamics obtained by DFS has the potential to shed new light and provide readouts to assess the pathophysiological status of cells for diagnostic purposes.

We used the dispersion relation to study actin and microtubule polymerization and depolymerization dynamics in live cells. DFS is a full-field and tracking-free method, which is ideally suited for studying dynamics of both continuous

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**Figure 4** Long-term effect of cyto-D treatment on MEFs.  
**Notes:** (A) Actin-GFP image of a transfected MEF cell. (B–D) The same cell at different points in time, as indicated, after adding cyto-D. (E–H) Dispersion maps of $\Gamma$ ($q_x$,$q_y$) associated with images A–D, with two axes of symmetry shown. (I–L) Dispersion-relation curves plotted along the two axes ($\theta_x$, $\theta_y$), and azimuthally averaged, as indicated. Immediately after cyto-D was applied, the transport became diffusive ($q^2$). However, with time, the deterministic trend ($q^1$) was observed again (K and L). All time-lapse images were acquired at 1 frame/second for 4.25 minutes using epifluorescence microscopy. $q_x$ corresponds to deterministic transport and $q_y$ corresponds to diffusion.  
**Abbreviations:** MEF, mouse embryonic fibroblast; cyto-D, cytochalasin D; GFP, green fluorescence protein; T, time.
and discrete structures inside living cells. While in this study we used MEF cells, DFS can be applied to any cell line with fluorescently labeled organelles. The ability to distinguish between diffusion and deterministic transport over broad spatiotemporal scales promises to shed new light on understanding many cell functions. The specific study presented here on cytoskeleton dynamics under the influence of various motor-protein inhibitors suggests cross talk between actin and microtubule transport. Since many basic and clinical questions related to actin- and microtubule-mediated transport are insufficiently understood, we anticipate that DFS will contribute meaningfully to such studies in the future.

Figure 5 Effects of MEF treatment with cyto-D and nocodazole.
Notes: (A) Actin-GFP image of a transfected MEF cell. (B and C) The same cell at different points in time, as indicated, after adding cyto-D. (D) Addition of nocodazole. (E and F) The same cell at different points in time after adding nocodazole. (G–L) Dispersion maps of $I(q, q_0)$ associated with images (A–F), with two axes of symmetry shown in (G). (M–R) Dispersion-relation curves plotted along the two axes ($\theta_1$, $\theta_2$), and azimuthally averaged, as indicated. The green lines show the theoretical curve for a $\sim q^2$ fit, or linear fit, which indicates deterministic transport, and $\sim q$, or quadratic fit, which indicates Brownian motion. Immediately after cyto-D was applied, the transport became diffusive (O), and later showed a deterministic trend (P). However, after the nocodazole treatment, diffusion became dominant (Q) and R). All time-lapse images were acquired at 1 frame/second for 4.25 minutes using epifluorescence microscopy. $q_0$ corresponds to deterministic transport and $q$ corresponds to diffusion.

Abbreviations: MEF, mouse embryonic fibroblast; cyto-D, cytochalasin D; GFP, green fluorescence protein; T, time.

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Disclosure
The authors report no conflicts of interest in this work.

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